

Electrical Theory

Impedance

PJM State & Member Training Dept.

Objectives



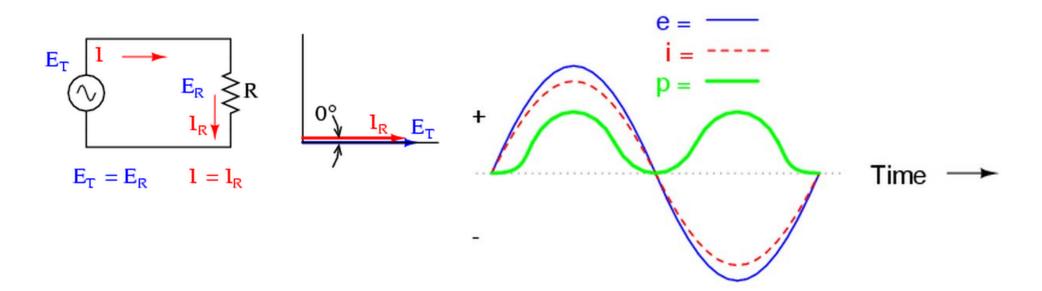
- Identify the components of Impedance in AC Circuits
- Calculate the total Impedance in AC Circuits
- Identify the characteristics of Phase Angles



Components of Impedance AC Circuits

Resistance

- Resistance: $R = \frac{E}{I}$
- A change in frequency has no effect on resistance
- Current through a resistor and the voltage drop across the resistor are always in phase



Resistance Characteristics

- In a purely resistive AC circuit:
 - Voltage and current cycles begin and end at the same time
 - Voltage and current peak values occur at the same time
- Relationship between current and voltage for resistance in an AC circuit is the same as it is in a DC circuit
- Measured values of current and voltage are the Root Mean Square (RMS) values of these quantities
- Only resistance consumes power in a circuit

 $\boldsymbol{P} = \boldsymbol{E}_{RMS} \boldsymbol{I}_{RMS} \cos \boldsymbol{\theta}$



Answer Questions 1 and 2

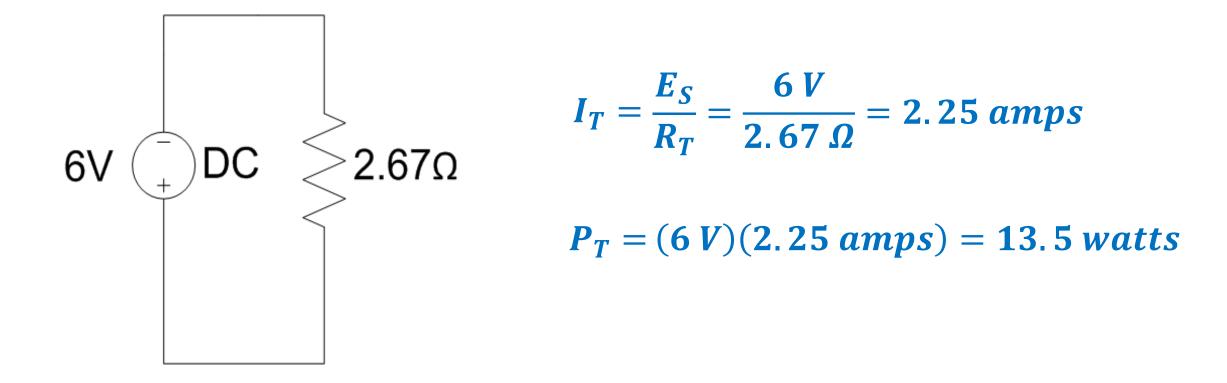
PJM State & Member Training Dept.

A circuit has a 133 ohm resistor connected to a 24 volt source. Determine the current flowing in the circuit:

E = IR

a)
$$I = \frac{E}{R} = \frac{24 V}{133 \Omega} = 0.18 amps$$

- A stereo receiver has a set of speakers, main and remote, for each channel
 - The speakers for each channel are connected in parallel to the receiver
 - The AC voltage across the speakers is 6.0 volts and the equivalent resistance is 2.67Ω
- Determine the total current supplied by the receiver and the power dissipated in the set of speakers



Inductive Reactance Characteristics

- An inductor's basis of operation is Faraday's law of electromagnetic induction
- An inductor develops a voltage that opposes a change in current
- Does not convert electrical energy into heat energy

Inductive Reactance Characteristics

- It is the result of induced voltage in a coil by the moving magnetic field created by current flow
- Current must be changing for voltage to be induced
- An inductor allows just enough current flow to produce a voltage equal to but opposing the source voltage
- Inductive reactance (X_L) is measured in ohms and determines how much RMS current exists in an inductor for a given RMS voltage across the inductor

Inductive Reactance

- Average power and average energy used by a inductor in an AC circuit is zero
 - a) When the voltage and current product is positive, the inductor is returning energy
 - b) When the voltage and current product is negative, energy is delivered to the inductor

Inductive Reactance

• Ohm's Law and inductive reactance:

 $E = (I)(X_L) \qquad X_L = 2\pi f L$

where,

E and I = RMS values for voltage and current

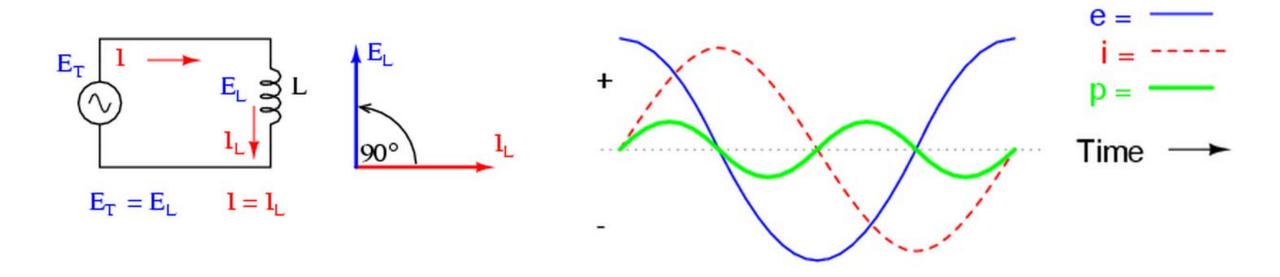
f = frequency (hertz)

L = inductance (henry)

- Increasing frequency increases inductive reactance
- As frequency increases, current changes more rapidly increasing the value of induced voltage

Inductive Reactance

In a purely inductive circuit, voltage leads the current by 90 degrees





Answer Questions 3-6

PJM State & Member Training Dept.

Calculate the inductive reactance of a circuit having a pure inductance of 50 millihenries with a frequency of 60 Hz

 $X_L = 2\pi f L = 2\pi (60 Hz)(0.05 H) = 18.85 \Omega$

Calculate the inductive reactance of a 2 henry inductance at 60 Hz

 $X_L = 2\pi f L$ $X_L = 2\pi (60)(2)$ $X_L = 754 \ \Omega$

A 0.16 H inductor is wired across the terminals of a generator that has a voltage of 120 volts and supplies a current of 5 amps

What is the frequency of the generator?

$$X_{L} = \frac{E}{I} = \frac{120 V}{5 A} = 24 \Omega$$
$$X_{L} = 2\pi f L$$
$$24 \Omega = 2\pi f (0.16 H)$$
$$f = \frac{24 \Omega}{2\pi (0.16 H)} = \frac{24 \Omega}{1.005} = 23.88 Hz$$

An 8.2 mH inductor is connected to an AC generator that is operating at 10.0 V and 60 Hz

What is the current supplied by the generator?

 $X_L = 2\pi f L = 2\pi (60 Hz)(0.0082 H) = 3.09 \Omega$

$$I_P = \frac{E}{X_L} = \frac{10 V}{3.09 \Omega} = 3.24 A$$

Capacitive Reactance

• Ohm's Law and capacitive reactance:

$$I = \frac{E}{X_C} \quad X_C = \frac{1}{2\pi fC}$$

where,

- E and I = RMS values for voltage and current
- f = frequency (hertz)
- C = capacitance (farads)
- Increasing frequency decreases capacitive reactance
- As frequency decreases, capacitive reactance becomes infinitely large, and a capacitor provides so much opposition to the motion of charges that there is no flow of current

Capacitive Reactance Characteristics

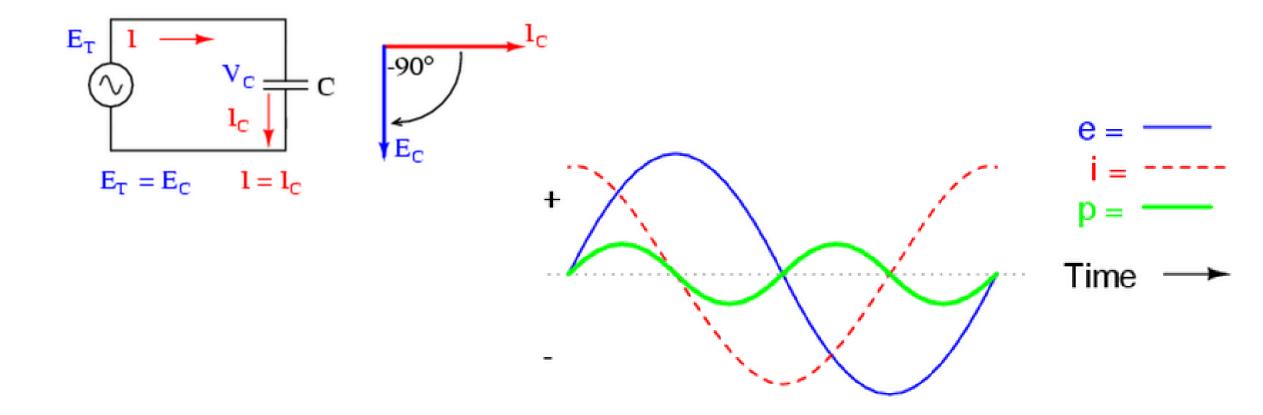
- In an AC circuit containing a capacitor, the polarity of the voltage continually reverses switching back and forth with the electrical charges also surging back and forth
- This constitutes an alternating current with charge flowing continuously
- A capacitor controls the current in an AC circuit by storing energy that produces voltage in a capacitor
- Capacitive reactance (XC) is measured in ohms and determines how much RMS current exists in a capacitor in response to a given RMS voltage across the capacitor

Capacitive Reactance Characteristics

- Does not convert electrical energy into heat energy
- It is the result of the capacitor storing energy that produces a voltage that opposes the source voltage and controls current
- Average power and average energy used by a capacitor in an AC circuit is zero
 - a) When the voltage and current product is positive, energy is delivered to the capacitor
 - b) When the voltage and current product is negative, the capacitor is returning energy

Capacitive Reactance

• In a purely capacitive circuit, current leads the voltage by 90 degrees



Capacitive Reactance

- Capacitors are used by utilities for:
 - Voltage regulation
 - Power factor correction
 - Inductance reduction
 - Measuring devices for protection systems
 - Communications for power line carriers
 - Filters for undesirable high frequency signals



Answer Questions 7-9

PJM State & Member Training Dept.

Calculate the capacitive reactance of a circuit having a capacitor of 400 microfarads with a frequency of 60 Hz

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi (60 \, Hz)(0.0004 \, F)} = 6.63 \, \Omega$$

- In a circuit, the capacitance of a capacitor is 1.65 microfarads, and the rms voltage of the generator is 50 volts
- What is the rms current in the circuit when the frequency is (a) 200 Hz and (b) 4500 Hz?

a)
$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi (200 \, Hz)(0.00000165 \, F)} = 482.3 \,\Omega$$

 $I_{RMS} = \frac{E_{RMS}}{X_C} = \frac{50 \, V}{482.3 \,\Omega} = 0.104 \,A$
b) $X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi (4500 \, Hz)(0.00000165 \, F)} = 21.44 \,\Omega$
 $I_{RMS} = \frac{E_{RMS}}{X_C} = \frac{50 \, V}{21.44 \,\Omega} = 2.33 \,A$

Calculate the current through a 1 μ farad capacitor, the effective value of voltage applied across the capacitor is 100 volts, and the frequency is 60 Hz

$$X_{C} = \frac{1}{2\pi fC} = \frac{1}{2\pi (60 \text{ Hz})(0.000001 \text{ F})} = 2652.6 \Omega$$

E 100 V

$$I = \frac{L}{X_C} = \frac{100 V}{2652.6 \Omega} = 0.0377 A$$

LabVolt Exercises

• Do LabVolt exercises 1.1, 1.2, 3.1, 3.3, 4.1 and 4.3



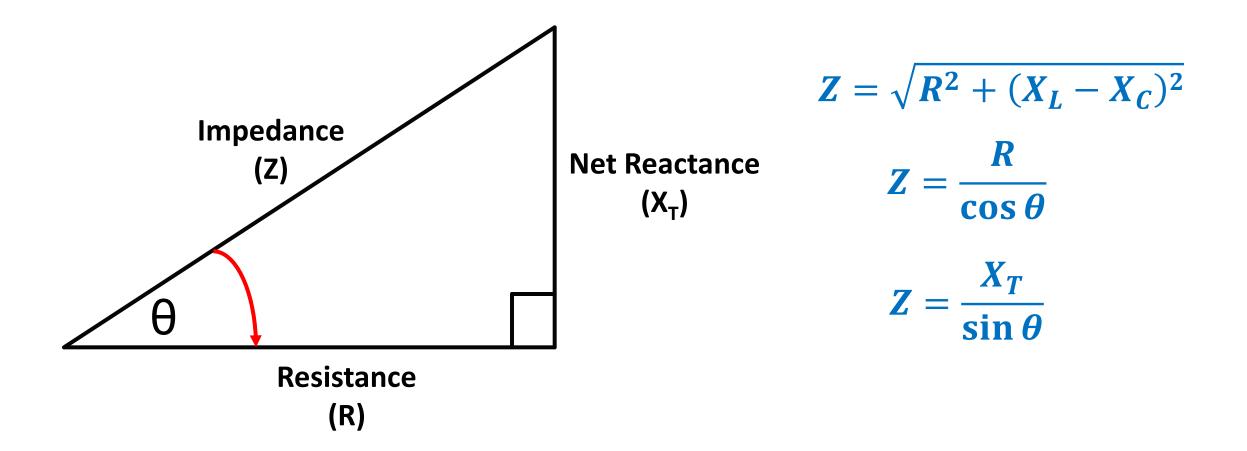
Total Impedance AC Circuits

- The impedance (Z) of an AC circuit is a complex sum of resistance (R) and net reactance (X_L- X_C)
- Impedance usually represented in polar form, with a magnitude and an angle (Z $\angle \theta$)
- Impedance is the total opposition to the flow of charge in an AC circuit
- A right triangle, called the impedance triangle is used to illustrate the relationship between AC resistance, reactance, and impedance

• Impedance (Z) is measured in ohms and defined as: $Z = \sqrt{R^2 + X_T^2}$

Where:

- $X_T = X_L X_C$ R = Resistance
- $X_T = Total Reactance$
- X_L = Inductive Reactance
- X_c = Capacitive Reactance
- X_L and X_C are 180° out of phase





Answer Questions 10 and 11

PJM State & Member Training Dept.

Given a RL circuit with a resistance of 5 ohms and a 35 ohm inductance at 60 Hz AC, find the (a) impedance (Z) and, (b) angle theta

a)
$$Z = \sqrt{R^2 + X_T^2} = \sqrt{5^2 + 35^2} = \sqrt{1444.78} = 35.36 \Omega$$

 $\cos \theta = \frac{R}{Z}$
b) $\theta = \cos^{-1} \frac{R}{Z} = \cos^{-1} \frac{5 \Omega}{35.36 \Omega} = \cos^{-1}(0.1414) = 81.87^\circ$

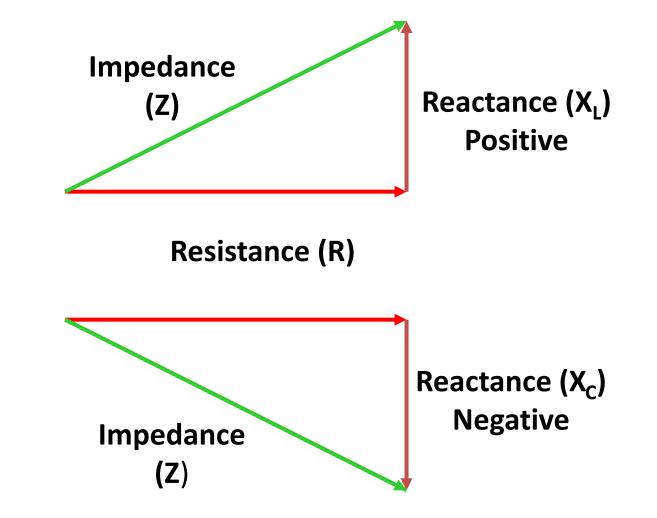
Given a RLC circuit where R is 5 ohms, $X_L = 35$ ohms, and X_C is 15 ohms, find the (a) impedance and (b) the angle theta

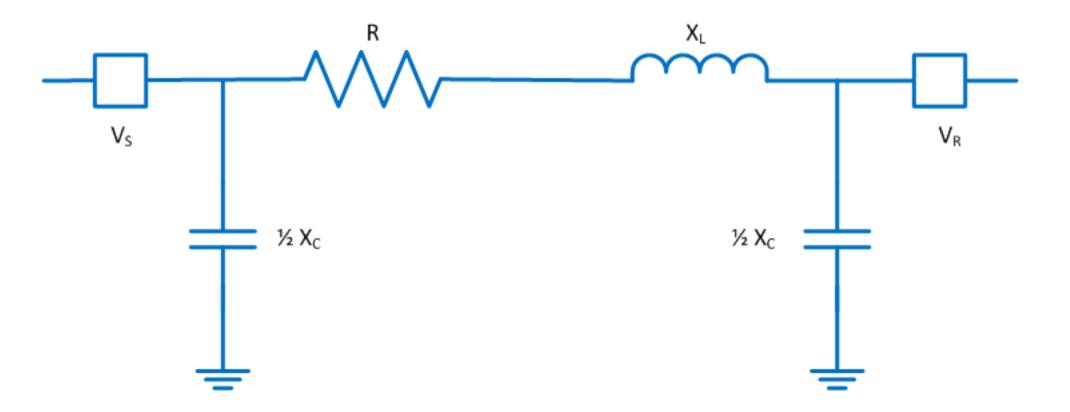
 $X_T = X_L - X_C = 35 \,\Omega - 15 \,\Omega = 20 \,\Omega$

a)
$$Z = \sqrt{R^2 + X_T^2} = \sqrt{5^2 + 20^2} = \sqrt{425} = 20.62 \Omega$$

b)
$$\theta = \cos^{-1} \frac{R}{Z} = \cos^{-1} \frac{5 \Omega}{20.62 \Omega} = \cos^{-1} 0.2425 = 75.97^{\circ}$$

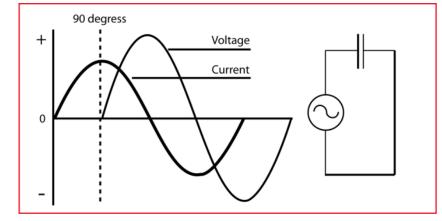
$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$
$$Z = \frac{R}{\cos \theta}$$
$$Z = \frac{X_T}{\sin \theta}$$



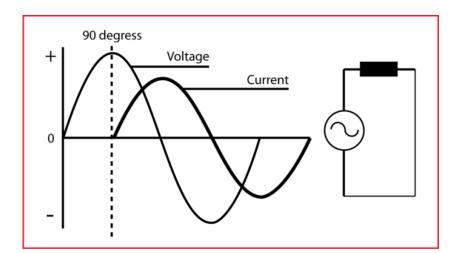


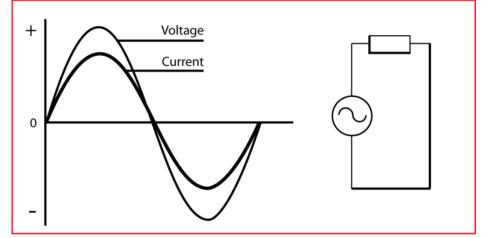
Values will depend on a line's length, cross-sectional area, and conductor spacing



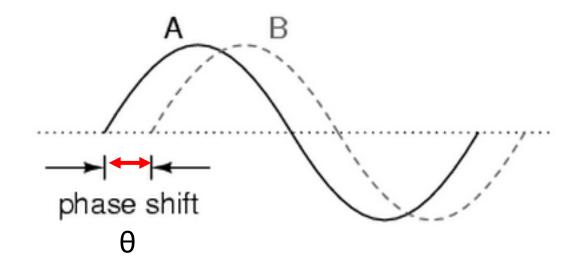


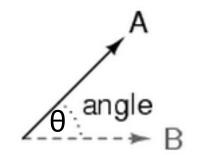
Phase Angle Part 3



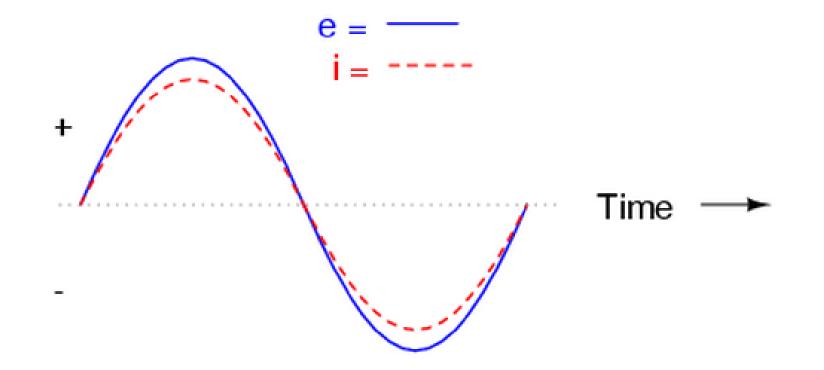


- Phase angle is defined as the angular separation between two phasors
- The spacing between the zero crossings of two waveforms also illustrates the phase angle (θ) of the circuit

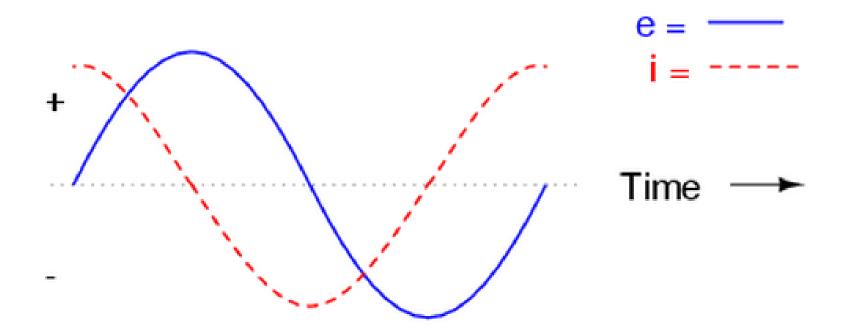




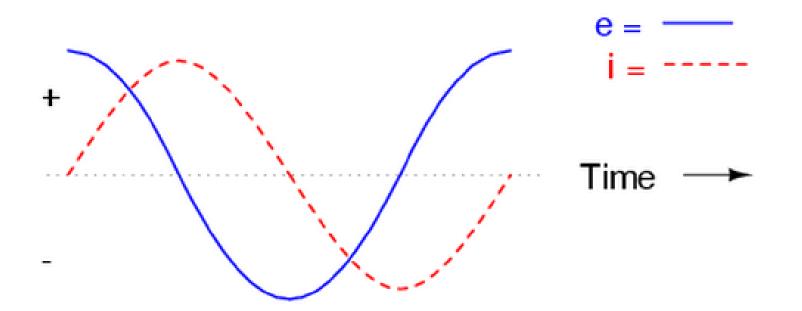
- The phase angle of a circuit is directly related to the impedance of the circuit
- For a purely resistive circuit, voltage and current will be in phase, and the phase angle will be zero



- A circuit has a leading phase angle when the current wave leads the voltage wave
- This occurs when the circuit is predominantly capacitive because of the energy storage of the electric field



- A circuit has a lagging phase angle when the current wave lags behind the voltage wave
- This occurs when the circuit is predominantly inductive because of the energy storage of the magnetic field



Summary

- Identified the components of Impedance in AC Circuits
- Calculated the total Impedance in AC Circuits
- Identified the characteristics of Phase Angles



Contact Information

PJM Client Management & Services Telephone: (610) 666-8980 Toll Free Telephone: (866) 400-8980 Website: <u>www.pim.com</u>



The Member Community is PJM's self-service portal for members to search for answers to their questions or to track and/or open cases with Client Management & Services

LabVolt Exercises

Do LabVolt exercises 5.2 and 5.4