

PJM Study of Carbon Pricing & Potential Leakage Mitigation Mechanisms Example Problem Formulations

Carbon Pricing Senior Task Force
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- All the example problem formulations are provided for illustrative purposes only and are not in any way representative of any market design proposal on behalf of PJM or any of its members.
- The formulation for the one-way border adjustment is adapted from CAISO's Energy Imbalance Market (EIM) Draft Final Proposal (published Sept. 23, 2013).
- The formulation for the two-way border adjustment is a possible extension of CAISO's EIM Draft Final Proposal.
- None of the formulations provided are unique and other formulations are possible.

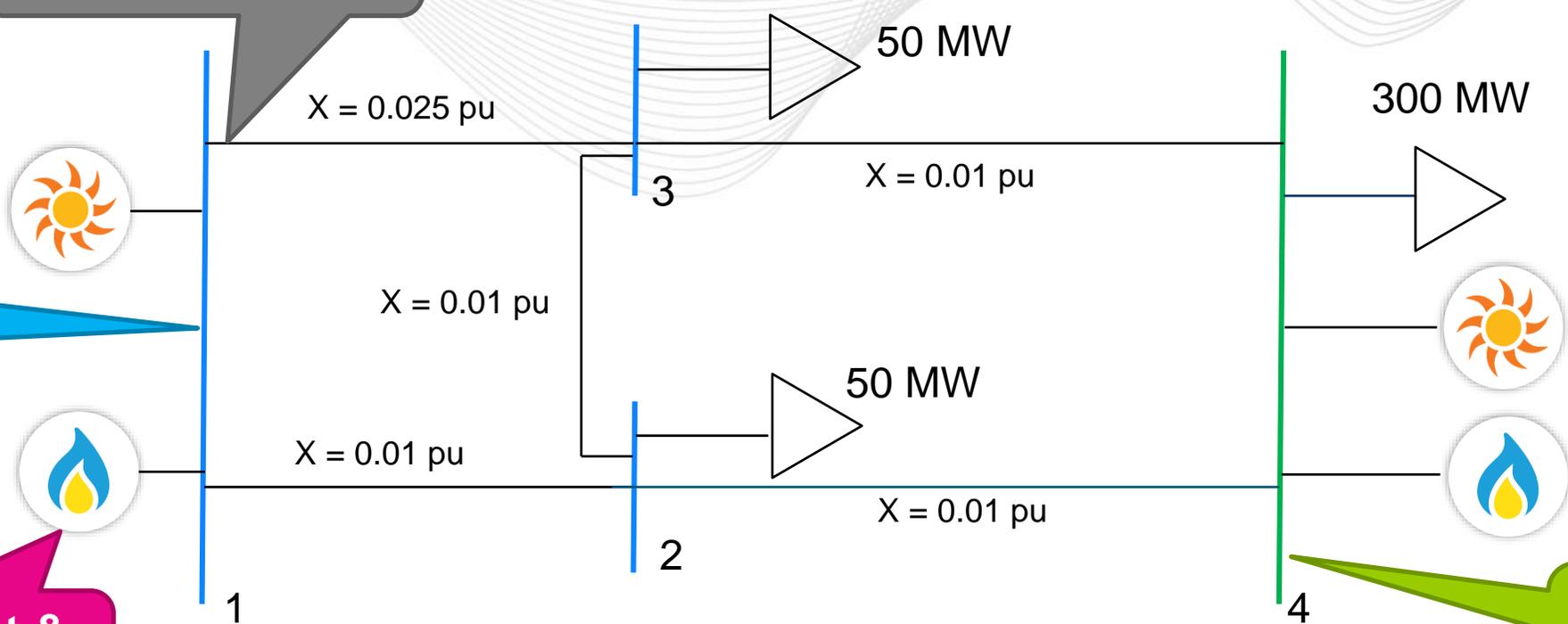
- 4 Bus System Example
- Notation
- Problem Formulations and Results
 - No Carbon Pricing
 - Carbon Pricing with No Border Adjustment
 - Carbon Pricing with One-Way Border Adjustment
 - Carbon Pricing with Two-Way Border Adjustment
- Border Adjustment Modeling in PLEXOS

All Line Limits are 225 MW

No-Carbon-Price Region

Less efficient & higher emissions

Cost Adder
(carbon price is \$1/short ton)



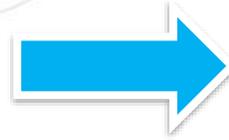
Carbon-Price Region

	Solar	Natural Gas	Solar	Natural Gas
EcoMax (MW)	100	400	100	400
Offer (\$/MWh)	0	30	0	20
GHG Cost (\$/MWh)	0	90	0	80

Unit Offers	}	C_{Solar}^{NC}	Solar unit offer (without GHG adder) in the no-carbon-price region
		C_{Gas}^{NC}	Gas unit offer (without GHG adder) in the no-carbon-price region
		C_{Solar}^C	Solar unit offer (without GHG adder) in the carbon-price region
		C_{Gas}^C	Gas unit offer (without GHG adder) in the carbon-price region
Unit Physical Dispatches	}	P_{Solar}^{NC}	Dispatch of the solar unit in the no-carbon-price region
		P_{Gas}^{NC}	Dispatch of the gas unit in the no-carbon-price region
		P_{Solar}^C	Dispatch of the solar unit in the carbon-price region
		P_{Gas}^C	Dispatch of the gas unit in the carbon-price region
Unit GHG Cost Adders	}	$C_{Solar\ GHG}^{NC}$	Solar unit GHG cost adder in the no-carbon-price region
		$C_{Gas\ GHG}^{NC}$	Gas unit GHG cost adder in the no-carbon-price region
		$C_{Solar\ GHG}^C$	Solar unit GHG cost adder in the carbon-price region
		$C_{Gas\ GHG}^C$	Gas unit GHG cost adder in the carbon-price region
Unit GHG Dispatches (MW amount being transferred to the other region)	}	$P_{Solar\ GHG}^{NC}$	Solar unit GHG dispatch in the no-carbon-price region
		$P_{Gas\ GHG}^{NC}$	Gas unit GHG dispatch in the no-carbon-price region
		$P_{Solar\ GHG}^C$	Solar unit GHG dispatch in the carbon-price region
		$P_{Gas\ GHG}^C$	Gas unit GHG dispatch in the carbon-price region
		θ_i	Bus voltage angle for bus i .
		$Flow_{i,j}$	MW flow on line from bus i to bus j .

Minimize Production Cost

$$\text{Minimize: } \left\{ \begin{array}{l} C_{Solar}^{NC} \cdot P_{Solar}^{NC} + C_{Gas}^{NC} \cdot P_{Gas}^{NC} + \\ C_{Solar}^C \cdot P_{Solar}^C + C_{Gas}^C \cdot P_{Gas}^C \end{array} \right\}$$



$$\text{Minimize: } \left\{ \begin{array}{l} 0 \cdot P_{Solar}^{NC} + 30 \cdot P_{Gas}^{NC} + \\ 0 \cdot P_{Solar}^C + 20 \cdot P_{Gas}^C \end{array} \right\}$$

Subject to:

Generator Constraints

$$\begin{aligned} 0 &\leq P_{Solar}^{NC} \leq 100 \\ 0 &\leq P_{Gas}^{NC} \leq 400 \\ 0 &\leq P_{Solar}^C \leq 100 \\ 0 &\leq P_{Gas}^C \leq 400 \end{aligned}$$

Line Constraints

$$\begin{aligned} -225 &\leq Flow_{12} \leq 225 \\ -225 &\leq Flow_{13} \leq 225 \\ -225 &\leq Flow_{23} \leq 225 \\ -225 &\leq Flow_{24} \leq 225 \\ -225 &\leq Flow_{34} \leq 225 \end{aligned}$$

$$\begin{aligned} 100 \cdot \theta_1 - 100 \cdot \theta_2 - Flow_{12} &= 0 \\ 40 \cdot \theta_1 - 40 \cdot \theta_3 - Flow_{13} &= 0 \\ 100 \cdot \theta_2 - 100 \cdot \theta_3 - Flow_{23} &= 0 \\ 100 \cdot \theta_2 - 100 \cdot \theta_4 - Flow_{24} &= 0 \\ 100 \cdot \theta_3 - 100 \cdot \theta_4 - Flow_{34} &= 0 \end{aligned}$$

DC Power Flow Equations

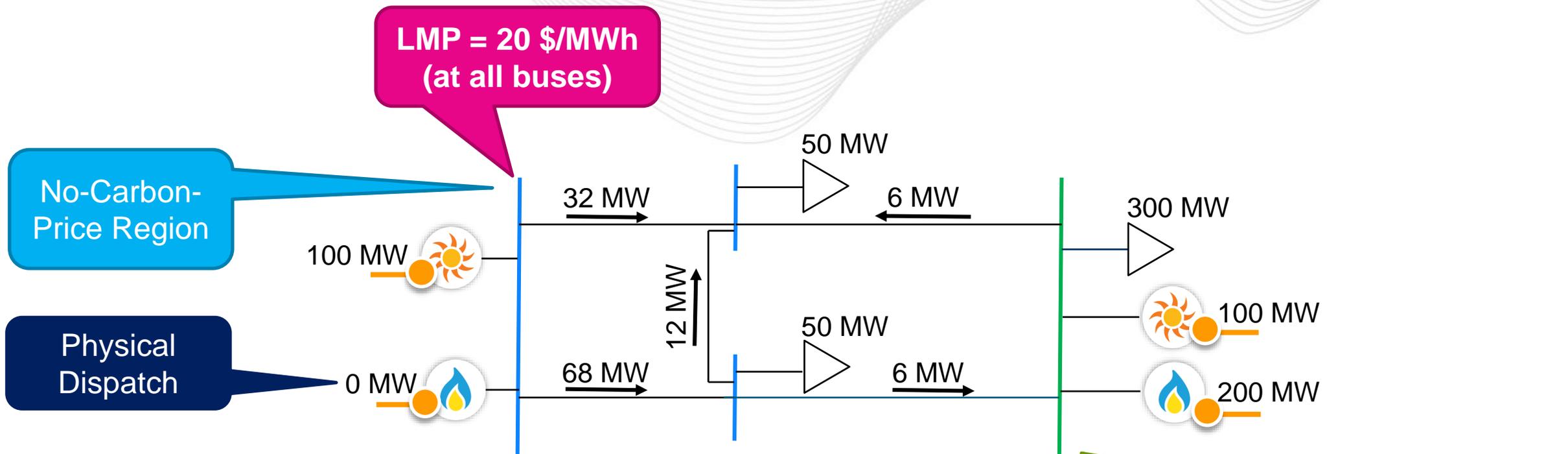
$$\begin{aligned} P_{Solar}^{NC} + P_{Gas}^{NC} - Flow_{12} - Flow_{13} &= 0 \\ Flow_{12} - Flow_{23} - Flow_{24} - 50 &= 0 \\ Flow_{13} + Flow_{23} - Flow_{34} - 50 &= 0 \\ P_{Solar}^C + P_{Gas}^C + Flow_{24} + Flow_{34} - 300 &= 0 \end{aligned}$$

Nodal Balance Equations

$$LMP_i = \lambda_i \quad \text{for all } i \text{ buses}$$

where:

λ_i = shadow price of the nodal balance constraint for bus i



**LMP = 20 \$/MWh
(at all buses)**

No-Carbon-Price Region

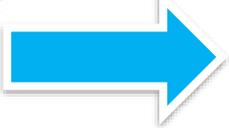
Physical Dispatch

Carbon-Price Region

	Solar	Gas	Solar	Gas
Offer (\$/MWh)	0	30	0	20
GHG Cost (\$/MWh)	0	90	0	80

Same Equations With Additional GHG Cost Adders

$$\text{Minimize: } \left\{ \begin{aligned} & C_{Solar}^{NC} \cdot P_{Solar}^{NC} + C_{Gas}^{NC} \cdot P_{Gas}^{NC} + \\ & (C_{Solar}^C + C_{Solar}^{C\ GHG}) \cdot P_{Solar}^C + \\ & (C_{Gas}^C + C_{Gas}^{C\ GHG}) \cdot P_{Gas}^C \end{aligned} \right\}$$



$$\text{Minimize: } \left\{ \begin{aligned} & 0 \cdot P_{Solar}^{NC} + 30 \cdot P_{Gas}^{NC} + \\ & (0 + 0) \cdot P_{Solar}^C + \\ & (20 + 80) \cdot P_{Gas}^C \end{aligned} \right\}$$

GHG Cost Added to Generator Offer

Subject to:

$0 \leq P_{Solar}^{NC} \leq 100$	$100 \cdot \theta_1 - 100 \cdot \theta_2 - Flow_{12} = 0$
$0 \leq P_{Gas}^{NC} \leq 400$	$40 \cdot \theta_1 - 40 \cdot \theta_3 - Flow_{13} = 0$
$0 \leq P_{Solar}^C \leq 100$	$100 \cdot \theta_2 - 100 \cdot \theta_3 - Flow_{23} = 0$
$0 \leq P_{Gas}^C \leq 400$	$100 \cdot \theta_2 - 100 \cdot \theta_4 - Flow_{24} = 0$
	$100 \cdot \theta_3 - 100 \cdot \theta_4 - Flow_{34} = 0$
$-225 \leq Flow_{12} \leq 225$	$P_{Solar}^{NC} + P_{Gas}^{NC} - Flow_{12} - Flow_{13} = 0$
$-225 \leq Flow_{13} \leq 225$	$Flow_{12} - Flow_{23} - Flow_{24} - 50 = 0$
$-225 \leq Flow_{23} \leq 225$	$Flow_{13} + Flow_{23} - Flow_{34} - 50 = 0$
$-225 \leq Flow_{24} \leq 225$	$P_{Solar}^C + P_{Gas}^C + Flow_{24} + Flow_{34} - 300 = 0$
$-225 \leq Flow_{34} \leq 225$	

$$LMP_i = \lambda_i \quad \text{for all } i \text{ buses}$$

where:

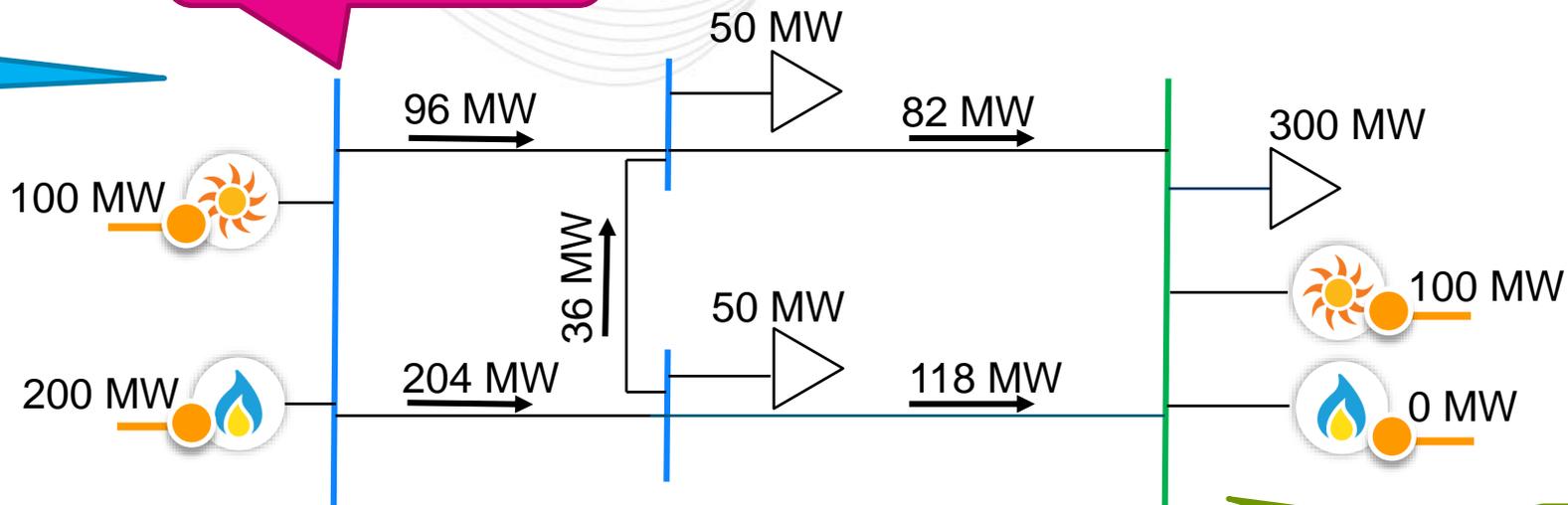
λ_i = shadow price of the nodal balance constraint for bus i

Results – Carbon Pricing No Border Adjustment

**LMP = 30 \$/MWh
(at all buses)**

No-Carbon-Price Region

Physical Dispatch



Carbon-Price Region

	Solar	Gas	Solar	Gas
Offer (\$/MWh)	0	30	0	20
GHG Cost (\$/MWh)	0	90	0	80

Net Offer = 20 \$/MWh + 80 \$/MWh

Problem Formulation – Carbon Pricing with One-Way Border Adjustment*

*Adapted from CAISO's Energy Imbalance Market (EIM) Draft Final Proposal (published Sept. 23, 2013)

Additional Terms

Minimize: {

$$C_{Solar}^{NC} \cdot P_{Solar}^{NC} + C_{Gas}^{NC} \cdot P_{Gas}^{NC} + C_{Solar\ GHG}^{NC} \cdot P_{Solar\ GHG}^{NC} + C_{Gas\ GHG}^{NC} \cdot P_{Gas\ GHG}^{NC} + (C_{Solar}^C + C_{Solar\ GHG}^C) \cdot P_{Solar}^C + (C_{Gas}^C + C_{Gas\ GHG}^C) \cdot P_{Gas}^C \}$$

Physical Dispatch
 P_{Gas}^{NC}

GHG Dispatch
 $P_{Gas\ GHG}^{NC}$

Minimize: {

$$0 \cdot P_{Solar}^{NC} + 30 \cdot P_{Gas}^{NC} + 0 \cdot P_{Solar\ GHG}^{NC} + 90 \cdot P_{Gas\ GHG}^{NC} + (0 + 0) \cdot P_{Solar}^C + (20 + 80) \cdot P_{Gas}^C \}$$

Subject to:

$$\begin{aligned} 0 \leq P_{Solar}^{NC} \leq 100 & \quad 100 \cdot \theta_1 - 100 \cdot \theta_2 - Flow_{12} = 0 \\ 0 \leq P_{Gas}^{NC} \leq 400 & \quad 40 \cdot \theta_1 - 40 \cdot \theta_3 - Flow_{13} = 0 \\ 0 \leq P_{Solar}^C \leq 100 & \quad 100 \cdot \theta_2 - 100 \cdot \theta_3 - Flow_{23} = 0 \\ 0 \leq P_{Gas}^C \leq 400 & \quad 100 \cdot \theta_2 - 100 \cdot \theta_4 - Flow_{24} = 0 \\ & \quad 100 \cdot \theta_3 - 100 \cdot \theta_4 - Flow_{34} = 0 \\ -225 \leq Flow_{12} \leq 225 & \\ -225 \leq Flow_{13} \leq 225 & \quad P_{Solar}^{NC} + P_{Gas}^{NC} - Flow_{12} - Flow_{13} = 0 \\ -225 \leq Flow_{23} \leq 225 & \quad Flow_{12} - Flow_{23} - Flow_{24} - 50 = 0 \\ -225 \leq Flow_{24} \leq 225 & \quad Flow_{13} + Flow_{23} - Flow_{34} - 50 = 0 \\ -225 \leq Flow_{34} \leq 225 & \quad P_{Solar}^C + P_{Gas}^C + Flow_{24} + Flow_{34} - 300 = 0 \end{aligned}$$

Subject to additional constraints:

$$\begin{aligned} 0 \leq P_{Solar\ GHG}^{NC} \leq P_{Solar}^{NC} \\ 0 \leq P_{Gas\ GHG}^{NC} \leq P_{Gas}^{NC} \end{aligned}$$

GHG Limit Constraints:
Cannot allocate more than what is physically dispatched

Allocation Constraint: Total allocation plus load must be greater than or equal to total generation in the no-carbon-price region

$$P_{Solar}^{NC} + P_{Gas}^{NC} \leq P_{Solar\ GHG}^{NC} + P_{Gas\ GHG}^{NC} + 100$$

$LMP_i = \lambda_i$ for all i buses in the carbon-price region

$LMP_j = \lambda_j + \eta$ for all j buses in the no-carbon-price region

$LMP_{Carbon} = -\eta$

where:

λ_i = shadow price of the nodal balance constraint for bus i

η = shadow price of the allocation constraint

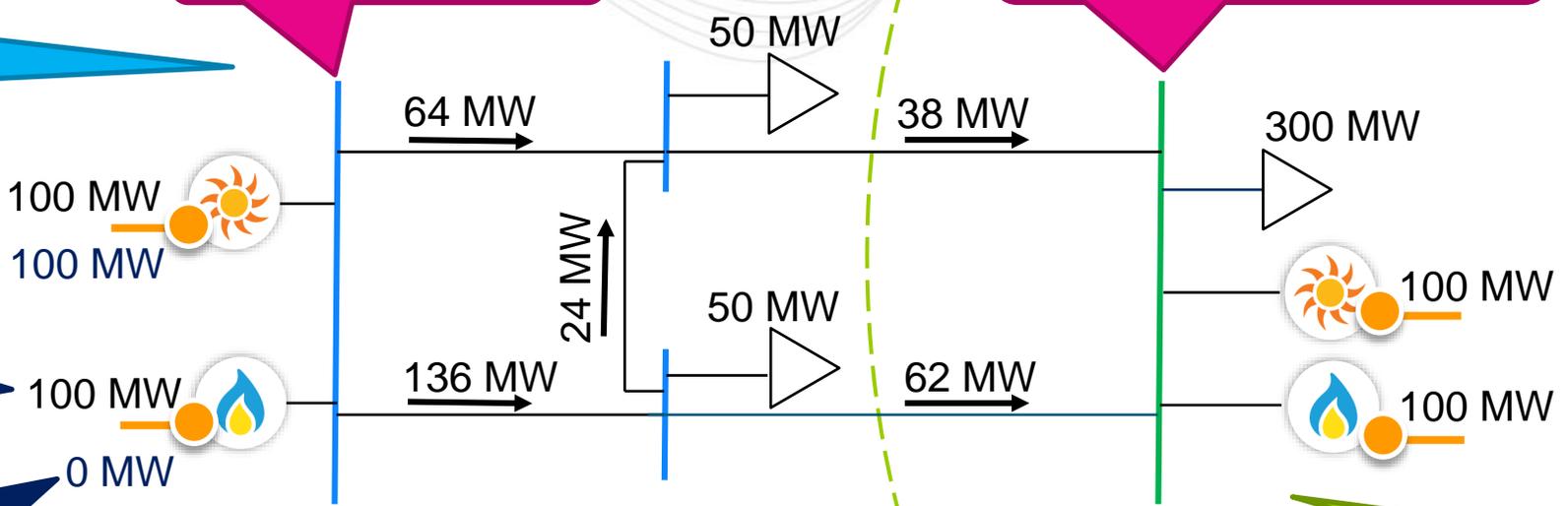
No-Carbon-Price Region

Physical Dispatch

GHG Dispatch (serving the carbon-price region)

LMP = 30 \$/MWh

LMP = 100 \$/MWh
LMP_{CARBON} = 70 \$/MWh



	Solar	Gas	Solar	Gas
Offer (\$/MWh)	0	30	0	20
GHG Cost (\$/MWh)	0	90	0	80

Carbon-Price Region

Minimize: {

$$C_{Solar}^{NC} \cdot P_{Solar}^{NC} + C_{Gas}^{NC} \cdot P_{Gas}^{NC} +$$

$$C_{Solar\ GHG}^{NC} \cdot P_{Solar\ GHG}^{NC} + C_{Gas\ GHG}^{NC} \cdot P_{Gas\ GHG}^{NC} +$$

$$(C_{Solar}^C + C_{Solar\ GHG}^C) \cdot P_{Solar}^C + (C_{Gas}^C + C_{Gas\ GHG}^C) \cdot P_{Gas}^C -$$

$$C_{Solar\ GHG}^C \cdot P_{Solar\ GHG}^C - C_{Gas\ GHG}^C \cdot P_{Gas\ GHG}^C$$

}



Minimize: {

$$0 \cdot P_{Solar}^{NC} + 30 \cdot P_{Gas}^{NC} +$$

$$0 \cdot P_{Solar\ GHG}^{NC} + 90 \cdot P_{Gas\ GHG}^{NC} +$$

$$(0 + 0) \cdot P_{Solar}^C + (20 + 80) \cdot P_{Gas}^C -$$

$$0 \cdot P_{Solar\ GHG}^C - 80 \cdot P_{Gas\ GHG}^C$$

}

Subject to:

Additional Terms

$0 \leq P_{Solar}^{NC} \leq 100$	$100 \cdot \theta_1 - 100 \cdot \theta_2 - Flow_{12} = 0$
$0 \leq P_{Gas}^{NC} \leq 400$	$40 \cdot \theta_1 - 40 \cdot \theta_3 - Flow_{13} = 0$
$0 \leq P_{Solar}^C \leq 100$	$100 \cdot \theta_2 - 100 \cdot \theta_3 - Flow_{23} = 0$
$0 \leq P_{Gas}^C \leq 400$	$100 \cdot \theta_2 - 100 \cdot \theta_4 - Flow_{24} = 0$
	$100 \cdot \theta_3 - 100 \cdot \theta_4 - Flow_{34} = 0$
$-225 \leq Flow_{12} \leq 225$	
$-225 \leq Flow_{13} \leq 225$	$P_{Solar}^{NC} + P_{Gas}^{NC} - Flow_{12} - Flow_{13} = 0$
$-225 \leq Flow_{23} \leq 225$	$Flow_{12} - Flow_{23} - Flow_{24} - 50 = 0$
$-225 \leq Flow_{24} \leq 225$	$Flow_{13} + Flow_{23} - Flow_{34} - 50 = 0$
$-225 \leq Flow_{34} \leq 225$	$P_{Solar}^C + P_{Gas}^C + Flow_{24} + Flow_{34} - 300 = 0$

Subject to additional constraints:

$$0 \leq P_{Solar\ GHG}^{NC} \leq P_{Solar}^{NC}$$

$$0 \leq P_{Gas\ GHG}^{NC} \leq P_{Gas}^{NC}$$

$$0 \leq P_{Solar\ GHG}^C \leq P_{Solar}^C$$

$$0 \leq P_{Gas\ GHG}^C \leq P_{Gas}^C$$

GHG Limit Constraints:
Cannot allocate more than what is physically dispatched

Allocation Constraint

$$P_{Solar\ GHG}^C + P_{Gas\ GHG}^C \leq$$

$$P_{Solar\ GHG}^{NC} + P_{Gas\ GHG}^{NC} + P_{Solar}^C + P_{Gas}^C - 300$$

$LMP_i = \lambda_i - \eta$ for all i buses in the carbon-price region

$LMP_j = \lambda_j$ for all j buses in the no-carbon-price region

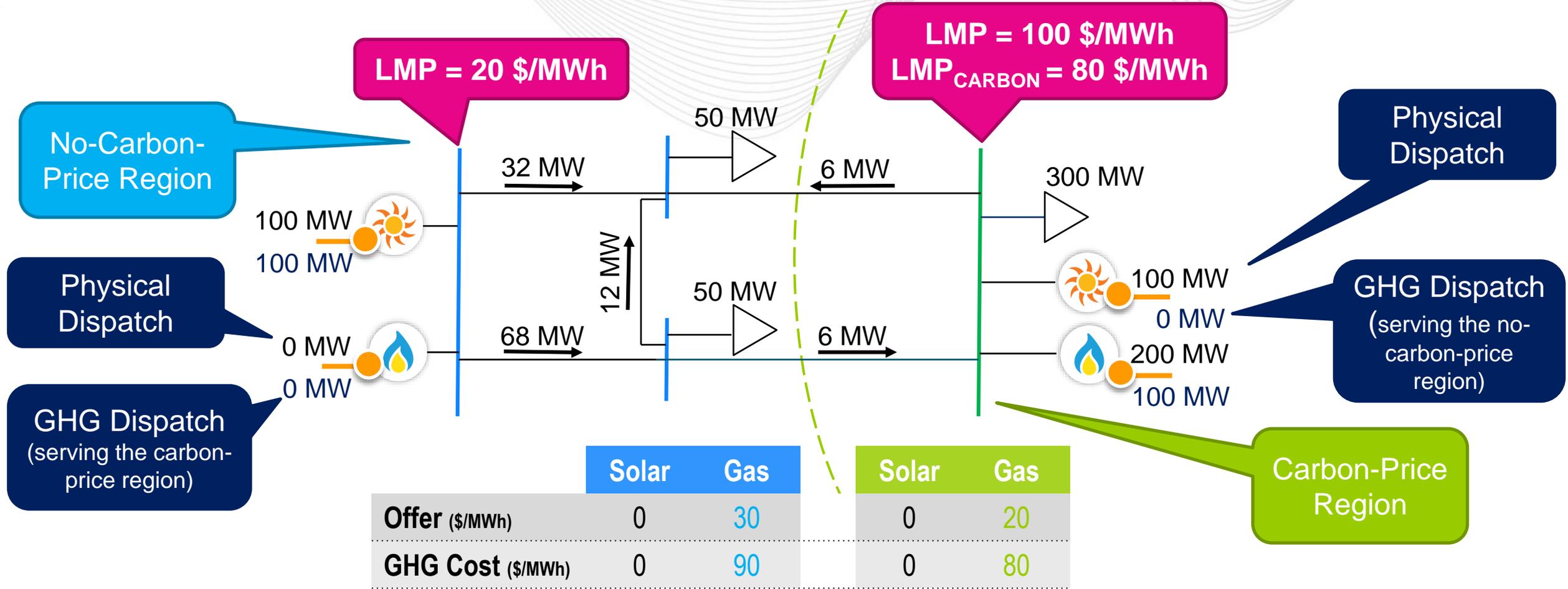
$LMP_{Carbon} = -\eta$

where:

λ_i = shadow price of the nodal balance constraint for bus i

η = shadow price of the allocation constraint

Results – Carbon Pricing With Two-Way Border Adjustment



- In order to model the border adjustment cases in PLEXOS, the following methodology was used.
- Note: PLEXOS is a production cost model, and is not meant to represent any actual implementation.

Methodology:

- In PLEXOS, each fossil fuel burning generator was modeled as having two fuels available to it:
 - One fuel had a cost that included the cost of carbon emissions.
 - One fuel had a cost that did not include the cost of carbon emissions.

- Carbon-Price Sub-Region:
 - Each fossil fuel generator was restricted to use only the fuel that included the cost of carbon emissions.
- Rest of RTO Sub-Region:
 - Each fossil fuel generator was restricted to use only the fuel that did not include the cost of carbon emissions.

- Carbon-Price Sub-Region:
 - Each fossil fuel generator was restricted to use only the fuel that included the cost of carbon emissions.
- Rest of RTO Sub-Region:
 - Each fossil fuel generator was allowed to use either fuel available to it.
- Border Adjustment Constraint:
 - A custom constraint was added to the model that restricted the amount of generation from fossil fuel generators using fuels that did not include the cost of carbon emissions to the amount of load in the Rest of RTO sub-region.

- Carbon-Price Sub-Region:
 - Each fossil fuel generator was allowed to use either fuel available to it.
- Rest of RTO Sub-Region:
 - Each fossil fuel generator was allowed to use either fuel available to it.
- Border Adjustment Constraint:
 - A custom constraint was added to the model that restricted the amount of generation from fossil fuel generators using fuels that did not include the cost of carbon emissions to the amount of load in the Rest of RTO sub-region.